

# Multiple View Geometry

## Chapter 4 Estimation - 2D Projective Transformations

Tomohiro Yasuda

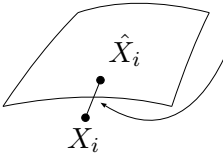
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## 4.2 Different cost functions (5/6)

The image correspondences define an algebraic variety in  $\mathcal{R}^4$ , and estimating a homography becomes the task of finding a variety.

- ▶ A coordinate  $X_i$  in  $\mathcal{R}^4$  is the pair of image points  $(x_i, y_i), (x'_i, y'_i)$ .
- ▶  $\mathbf{x}'_i \times (\mathbf{H} \mathbf{x}_i) = \mathbf{0}$  presents the intersection  $X_i$  of two quadrics.
- ▶ A variety  $\mathcal{V}_H$  passes (or most nearly passes) through the points  $X_i$ .

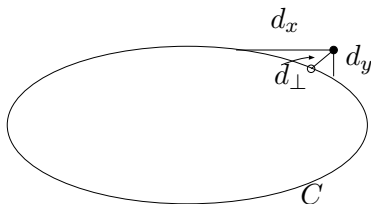
Perpendicular distance:


$$\begin{aligned}d_{\perp}(X_i, \mathcal{V}_H) &= \|X_i - \hat{X}_i\|^2 \\&= (x_i - \hat{x}_i)^2 + (y_i - \hat{y}_i)^2 + (x'_i - \hat{x}'_i)^2 + (y'_i - \hat{y}'_i)^2 \\&= \frac{d(\mathbf{x}, \hat{\mathbf{x}}_i)^2 + d(\mathbf{x}'_i, \hat{\mathbf{x}}'_i)^2}{\text{projection error}}\end{aligned}$$

$\hat{X}_i$ : the closest point to  $X_i$  lying on the variety  $\mathcal{V}_H$ .

## 4.2 Different cost functions (6/6)

Conic analogue :



- ▶  $d_{\perp}(X, C)^2 \leq d_x(X, C)^2 + d_y(X, C)^2$
- ▶ A conic can be estimated by minimizing  $\sum_i d_{\perp}(x_i, C)^2$ .
- ▶ Minimizing  $\sum_i d_{\perp}(x_i, C)^2$  cannot be achieved by a linear solution.